

A hierarchical approach to aligning collinear regions of genomes

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Received on February 4, 2002; revised on May 9, 2002; accepted on May 21, 2002

ABSTRACT

Motivation: As a first approximation, similarity between two long orthologous regions of genomes can be represented by a chain of local similarities. Within such a chain, pairs of successive similarities are collinear (nonconflicting), i.e. segments involved in the *n*th similarity precede in both sequences segments involved in the (n + 1)th similarity. However, when all similarities between two long sequences are considered, usually there are many conflicts between them. Although some conflicts can be avoided by masking transposons or low-complexity sequences, selecting only those similarities that reflect orthology and, thus, belong to the evolutionarily true chain is not trivial.

Results: We propose a simple, hierarchical algorithm of finding the true chain of local similarities. Starting from similarities with low *P*-values, we resolve each pairwise conflict by deleting a similarity with a higher *P*-value. This greedy approach constructs a chain of similarities faster than when a chain optimal with respect to some global criterion is sought, and makes more sense biologically.

Availability: A software tool OWEN based on the proposed approach is described in the accompanying note and is freely available at ftp://ftp.ncbi.nih.gov/pub/ kondrashov/owen.

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Supplementary information: Algorithm Chain and examples of chains of local similarities are available at ftp://ftp. ncbi.nih.gov/pub/kondrashov/owen/extra.

INTRODUCTION

Since all modern cells originated from the common ancestor (Doolittle, 2000), similarity can be found between every two genomes. However, the nature of this similarity depends strongly on the evolutionary distance. Gene order is poorly conserved between phylogenetically remote genomes, despite strong conservation of some orthologous genes (Wolf *et al.*, 2001). Comparing such genomes mostly means comparing unordered sets of protein sequences they encode.

In contrast, the order of orthologous genes is partially preserved between less distant genomes. In particular, regions of large-scale collinearity exist within all vertebrates (Venkatesh *et al.*, 2000) and all flowering plants (Eckardt, 2001). Thus, and since protein-coding exons constitute only a minority of the genomes of multicellular eukaryotes, these genomes must be compared by aligning their long, collinear regions (Miller, 2001). Finding such regions is an important problem (Hannenhalli and Pevzner, 1999; Zafar *et al.*, 2001)), which is not addressed here.

The degree of similarity between collinear regions of not-too-similar genomes is highly variable. Nearlyidentical segments alternate with those possessing no meaningful similarity (Jareborg *et al.*, 1999; Shabalina and Kondrashov, 1999). Thus, gene order is much more conservative than many nucleotide sites. Comparison of such genomes (e.g. of human and mouse) is better done in terms of sets of local similarities, and some regions should remain unaligned (Schwartz *et al.*, 2000; Miller, 2001). Of course, for pairs of very similar genomes, such as human and chimpanzee, global alignment makes perfect sense (e.g. Kent and Zahler, 2000).

Local similarities between orthologous segments of genome regions with large-scale collinearity are also mostly collinear (successive, non-conflicting), i.e. follow in the same order in both genomes (Schwartz *et al.*, 2000). In other words, macrocollinearity usually implies microcollinearity (Rossberg *et al.*, 2001) because the rate of divergence of rapidly evolving segments of genomes exceeds the rates of processes that disrupt microcollinearity, such as evolution due to duplications, inversions, transpositions, and convergence. Biologically, orthologous local similarities correspond either to units of function and selective constraint or, perhaps, to cold

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spots of mutation (Shabalina *et al.*, 2001). Still, when all local similarities between two long sequences are considered, usually there are numerous conflicts between them, although many conflicts involve rogue similarities between transposons and microsatellites, which can be recognized and masked (Miller, 2001).

Thus, although overall similarity between two macrocollinear genome regions can be mostly represented by the 'evolutionarily true' chain of microcollinear local similarities between their orthologous segments (Schwartz *et al.*, 2000; Shabalina *et al.*, 2001), finding local similarities that belong to this chain is not trivial. We will concentrate on this task, and treat the procedure of finding individual local similarities (e.g. Smith and Waterman, 1981; Lipman and Pearson, 1985; Altschul *et al.*, 1997; Zhang *et al.*, 1998; Arslan *et al.*, 2001) as a parameter.

In order to find a chain of local similarities, one must resolve all conflicts by erasing some conflicting local similarities completely or, if this is enough to resolve a conflict, by trimming them. Schwartz *et al.* (2000) described two methods of finding the true chain, both of which seek the chain which is optimal as a whole, i.e. maximizes some global score. In this paper, we propose another approach, which does not seek the optimal chain. Instead, we resolve each pairwise conflict that needs to be resolved in favor of the stronger local similarity. The presentation will be in terms of pairwise comparison, and our software tool OWEN (Ogurtsov *et al.*, 2002) currently handles only two genomes, although multiple genomes can be compared in the same way.

INFORMAL OVERVIEW OF THE APPROACH

Our simple, hierarchical, greedy approach is motivated by an observation that the pattern of similarity between long collinear regions of moderately similar genomes is rather different from that between moderately similar relatively short DNA or protein sequences. In the second case, the degree of similarity is often rather uniform, and parts of the global alignment which are significant *per se* cover only a small fraction of sequences. Thus, we cannot proceed greedily and need to optimize some global scoring function of the whole alignment. Building blocks of alignments of uniformly similar sequences are matches of individual letters, and conflicts between them are ubiquitous.

In contrast, moderate genome-level similarity is patchy, and building blocks of genome alignments are local similarities of some lengths, many of them individually statistically significant. When a pair of significant local similarities is in conflict, it indicates that a microcollinearitydisrupting event did happen during evolution of the compared genomes from the common ancestor (Figure 1). If so, two possibilities emerge.



Fig. 1. Types of conflicts between local similarities, shown as diagonals on the dot-matrix. (a) A severe conflict due to similar segments appearing in the opposite orders in the two sequences. (b) A severe conflict due to complete overlap of similar segments. (c) A mild conflict due to partial overlap of similar segments. Here, the conflicting similarities can be reconciled, by trimming their ends.

First, microcollinearity could have been violated due to local convergent evolution or to insertion, into one genome, of a repetitive sequence that is also present, at a different location, in the other genome. In this case one of the conflicting similarities does not involve orthologous sequences, and the pattern of orthology can still be presented by a chain. Second, microcollinearity could have been violated due to local reshuffling of segments of one or both sequences (Figure 1a) or to smallscale duplication(s) (Figure 1b). In this case, similarities between all orthologous segments do not form a chain.

In the first case, convergent evolution of sequences rarely makes them profoundly similar, so that orthology after such evolution is probably reflected by the strongest of the conflicting similarities. Insertion of a repeat can lead to a strong non-orthologous similarity, so it is better to mask repeats. However, even in this case the orthologous similarity can be stronger than any of several collinear non-orthologous similarities that conflict with it. If so, only individual resolution of conflicts between similarities will find the true chain (Figure 2).

In the second case, it is hard to say which of the conflicting similarities between orthologs must be kept in the chain, and which are to be erased (and, perhaps, recorded as 'footnotes' to the chain). Keeping the strongest similarity obviously makes sense.

Thus, the simplest rule of always keeping a stronger similarity is justified. In this paper, 'stronger' will mean



Fig. 2. Comparison of mouse (AF139987) and human (AF045555) sequences. The strongest, orthologous similarity *H* corresponds to exon 10 at locus Rfc2 (nucleotides 104514–104583 in the mouse sequence). Since non-orthologous similarities A_1 , A_2 , and A_3 constitute a chain with a score higher than that of a chain consisting of *H* alone, seeking the optimal as a whole chain using PipMaker (Schwartz *et al.*, 2000) or option Optimal in OWEN (Ogurtsov *et al.*, 2002) erases *H*. In contrast, resolving conflicts individually (option Greedy in OWEN) keeps *H* and erases A_1 , A_2 , and A_3 . Of course, if *H* were of secondary origin, and A_1 , A_2 , and A_3 were orthologous, only seeking the optimal as a whole chain would produce the correct result.

'having a lower *P*-value', but OWEN also allows human intervention in resolving individual conflicts (Ogurtsov *et al.*, 2002).

We can now formulate two basic principles of our approach to finding the true chain of local similarities:

(1) All conflicts between a statistically significant similarity and any number of weaker similarities are resolved in favor of the former. Thus, a similarity that does not conflict with any stronger similarity is always included into the chain.

(2) Principle 1 holds both for the whole sequences to be compared and for any pair of their orthologous subsequences ('fractality'). This is important because a similarity that is not significant when we compare two sequences of length 10^7 may become significant when the lengths are reduced (after other, stronger similarities have been found) to 10^3 . Thus, stronger similarities that do not conflict with them.

We call the chain of local similarities that is found by applying these principles backbone chain and hope that it is close to the evolutionarily true chain that reflects orthology. We start assembling the backbone chain from the strongest similarity, then add to it the strongest similarity that does not conflict with the first one, etc. Algorithmically, resolving conflicts individually is a stone that kills two birds.

First, we can use a greedy algorithm to select the backbone chain from any set of conflicting similarities. Second, we can create this set hierarchically, i.e. start from finding only very strong similarities and resolve all conflicts between them, then independently screen gaps between successive strong similarities for weaker similarities, etc. Thus, time-consuming screening of the whole dot-matrix for all weak similarities can be avoided.

FORMAL BACKGROUND

Here we introduce terminology that is necessary to define the backbone chain of local similarities between sequences U and V and to describe algorithms that find it. The segment of U(V) starting at the position b and ending at the position e is denoted U[b, e](V[b, e]).

Local similarities

A similarity H between U and V is a pair of segments $U[b_1, e_1]$ and $V[b_2, e_2]$ together with their alignment Al(H) and its score Score(H). These segments are referred to as U-domain and V-domain of the similarity, denoted Domain(H, U) (Domain(H, V)). The beginning and the end of the U-domain of H are Beg(H, U) and End(H, U), respectively, and the analogous notations are used for the V-domain. We do not specify an algorithm of finding H and the corresponding alignment, or how a score is assigned to the alignment. We only assume that the score increases with the number of matches, and decreases with the number of mismatches and gaps within the alignment, so that alignments with higher scores are 'better'. Later, some restrictions on alignments and their scores will be introduced.

Let *H* be a similarity between segments $U[b_1, e_1]$ and $V[b_2, e_2]$ and *G* be a similarity between $U[c_1, f_1]$ and $V[c_2, f_2]$, where $[c_1, f_1]$ is a subfragment of $[b_1, e_1]$ and $[c_2, f_2]$ is a subfragment of $[b_2, e_2]$. The similarity *G* is a *subsimilarity* of *H*, if Al(*G*) is a *subalignment* of Al(*H*), i.e. if Al(*G*) establishes the same correspondence between letters from $U[c_1, f_1]$ and $V[c_2, f_2]$ as does Al(*H*).

Chains of local similarities

Similarity H_1 precedes similarity H_2 (notation: $H_1 < H_2$) if the *U*-domain of H_1 precedes the *U*-domain of H_2 and the *V*-domain of H_1 precedes the *V*-domain of H_2 , i.e. if End(U, H_1) < Beg(U, H_2) and End(V, H_1) < Beg(V, H_2). Similarities H_1 and H_2 are in *conflict*, if neither H_1 precedes H_2 , nor H_2 precedes H_1 . Two similarities that are not in conflict are *collinear*. A *chain of similarities* is a set of similarities { H_1, H_2, \ldots, H_N } in which every two similarities are collinear, ordered according the relation of precedence. A similarity *H* is *collinear to the chain of similarities* $B = \{H_1, H_2, ..., H_N\}$, if it is collinear to all members of *B*. If *H* is collinear to *B*, *H follows kth similarity* of *B* (or *H can be included between kth and* (*k*+1)*th similarity* of *B*), where $1 \le k \le N - 1$, if $H_k < H < H_{k+1}$. For k = N this means that $H_N < H$, and for k = 0 this means that $H < H_1$.

Quality of a local similarity

The quality of a similarity can be characterized by its P-value (Durbin *et al.*, 1998; Mott, 2000). Informally, P-value of a similarity with score S within U and V is the probability that a pair of sequences with the same lengths and statistical properties as U and V contains at least one similarity of score S or higher. Thus, highly significant similarities have low P-values.

Let $P(S, L_1, L_2)$ be *P*-value of a similarity between sequences of lengths L_1 and L_2 with score *S*. For our purposes, the only important things are that $0 \le P \le 1$ and that $P(S, L_1, L_2)$ decreases with the increase of *S* and increases with L_1 and L_2 (informally, *P* 'normalizes' the score *S* by L_1 and L_2).

Reliability of similarities and their chains

Let *H* be a similarity between the fragments $U[c_1, f_1]$ and $V[c_2, f_2]$ and ε be a number between 0 and 1. Consider fragments $U[b_1, e_1]$ and $V[b_2, e_2]$ containing $U[c_1, f_1]$ and $V[c_2, f_2]$ respectively, i.e. $b_1 < c_1 < f_1 < e_1$ and $b_2 < c_2 < f_2 < e_2$. Similarity *H* is ε -reliable within $U[b_1, e_1]$ and $V[b_2, e_2]$ if $P(\text{Score}(H), e_1 - b_1 + 1, e_2 - b_2 + 1) < \varepsilon$.

Let *F* be a chain of similarities and *H* be a similarity from *F*. Consider a sub-chain F_H of *F* consisting of all similarities having scores higher than Score(*H*). The similarities from F_H divide the compared sequences into a series of pairs of segments and the similarity *H* belongs to one of the pairs of segments, say, $U[c_1, f_1]$ and $V[c_2, f_2]$. *H* is ε -reliable in *F* if *H* is ε -reliable within $U[c_1, f_1]$ and $V[c_2, f_2]$ (Figure 3). A chain of similarities *F* is ε reliable, if every similarity from *F* is ε -reliable in *F*.

Comparing sets of similarities

Let *R* be a set of similarities and $\langle R \rangle$ be the vector of scores of all similarities from *R*, in decreasing order. Let $\mathbf{r} = \langle r_1, r_2, \ldots \rangle$ and $\mathbf{s} = \langle s_1, s_2, \ldots \rangle$ be different vectors of scores (possibly, of different lengths). We will use the following lexicographic procedure to compare \mathbf{r} and \mathbf{s} . If for some $k r_k$ and s_k are different, $\mathbf{r} > \mathbf{s}$ ($\mathbf{r} < \mathbf{s}$) if $r_k > s_k(r_k < s_k)$ for the smallest *k* for which $r_k \neq s_k$. Otherwise, the longer vector is greater. Among two sets of similarities *R* and *Q*, *R* is *stronger* than *Q* if $\langle R \rangle > \langle Q \rangle$.



Fig. 3. The concept of ε -reliability of a similarity within a chain. Consider the chain $F = \{A_1, H, A_2, A_3\}$ and suppose that Score(H) < Score(A_2) < Score(A_3) < Score(A_1), so that $F_H = \{A_1, A_2, A_3\}, F_{A_2} = \{A_1, A_3\}, F_{A_3} = \{A_1\}, \text{ and } F_{A_1}$ is empty. Then, for example, A_2 is ε -reliable in F, if it is ε reliable in the marked region $U[\text{End}(A_1, U) + 1, \text{Beg}(A_3, U) - 1]$ * $V[\text{End}(A_1, V) + 1, \text{Beg}(A_3, V) - 1]$ between the similarities A_1 and A_3 . A_1 is ε -reliable in F, if it is ε -reliable within the whole sequences U and V.

Backbone chain

The chain of similarities F is a backbone chain of a set of similarities R (with a given P-value cutoff ε), if

- (a) F is ε -reliable,
- (b) every similarity from *F* belongs to *R* or is a subsimilarity of an element from *R*,
- (c) no other chain of similarities that satisfies (a) and (b) is better than *F*.

ALGORITHMS

Here we describe algorithms that find the backbone chain of similarities for sequences U and V at the level of reliability ε . The backbone chain is assembled from a given set R of N similarities. We assume that we never have to choose between two conflicting similarities of exactly the same score ('different scores condition'). This assumption allows us to avoid algorithmically clumsy and biologically unimportant situations that can be resolved by a heuristic. We also assume that we possess an algorithm SetLocSim (**int** BegU, BegV, EndU, EndV, **real** ε) that finds the set of all similarities with domains within U[BegU, EndU] and V[BegV, EndV], which are ε -reliable within this region.

We can proceed in two ways. First, we can find the backbone chain under assumption that all similarities from

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R have already been found. This is done by algorithm Chain. In the 'basic' case (the backbone chain contains only the initial similarities, and not their subsimilarities, Figure 3) run-time of Chain is $\sim N \cdot \log(T)$, where T is a number of similarities in the backbone chain. In the general case when some similarities overlap (their Udomains and/or V-domains have non-empty intersection) the run-time depends on the number of overlapping similarities, but usually is ~ $N \cdot \log(N)$, if conflicts between overlapping similarities can be resolved by constructing their subsimilarities.

Alternatively, we can avoid finding all elements of Rand proceed hierarchically. This is done by algorithm Fractal which generates (using SetLocSim) the necessary subsets of R and extracts, using a modification of Chain, from each of them the corresponding part of the backbone chain. In the worst (and extremely improbable) case the run-time of Fractal is the same as that of Chain. Normally, Fractal finds the backbone chain in time $c(\varepsilon) \cdot T$, where $c(\varepsilon)$ depends only on ε .

We start from describing Fractal, which is implemented in OWEN. After this, Chain will be described, first for the basic case and, finally, for the general case.

Algorithm fractal

Let us define S-restriction of a set of similarities as its subset consisting of all similarities with scores S or higher. One can find S-restriction K_S of a backbone chain K, knowing only S-restriction R_S of R. Indeed, let K be the backbone chain of R with a *P*-value cut-off ε . Then, for an arbitrary S, K_S coincides with the S-restriction of the backbone chain of R_S with the same ε ('greedy statement').

Fractal utilizes this statement in the following way. Let $P(S, \text{length}(U), \text{length}(V)) = \varepsilon$, so that S is the minimal score corresponding the *P*-values ε or lower within the whole sequences U and V. Fractal creates (using SetLocSim) the subset R_S of all similarities with the scores S or higher and constructs (using a modification of Chain) the S-restriction K_S of the backbone chain of R_S . Then, all elements of K_S belong to the final backbone chain for U and V. Thus, it is enough to process independently pairs of segments of U and V ('boxes') between successive similarities from K_S .

Fractal uses greedy paradigm twice. First, it hierarchically implements the greedy statement. Second, extraction of the backbone chain from the current set of similarities is performed by greedy algorithm Chain. Let us define box $\langle b_1, e_1, b_2, e_2 \rangle$ as a pair of segments $U[b_1, e_1]$ and $V[b_2, e_2]$ of sequences U and V. Fractal (Figure 4) operates with two global objects:

(i) the list of similarities BackboneChain (which finally contains the desired backbone chain) and

ALGORITHM Fractal (sequence U, sequence V, real epsilon) BEGIN // Prologue

- Mask transposones and low complexity regions in the sequences U and V;
- BackboneChain := empty; 2 3.
- MainBox := <1, length(U), 1, length(V)>;
- 4. WorkBoxList := $\{MainBox\}$:
- // Main Loop
- WHILE WorkBoxList is not empty DO BEGIN 5 CurrentBox := first (WorkBoxList);
- 7 delete CurrentBox from WorkBoxList;
- ProceedBox (CurrentBox, epsilon); 8.
- 9. END WHILE
- // Epilogue
 - RETURN BackboneChain;
- END_ALGORITHM

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(b)

3.

ALGORITHM ProceedBox (box CurrentBox, real epsilon) BEGIN

// Prologue

- // Let CurrentBox = $\langle b1, e1, b2, e2 \rangle$, i. e. it
- // corresponds to the segments U[b1, e1] and V[b2, e2].
- // We create temporary sequences U_Temp and V_Temp to be
- // compared and calculate their lengths L_U and L_V.
- $U_{Temp} = U[b1, e1];$
- L_U = length(U_Temp); $V_{Temp} = V[b1, e1];$ 2
 - $L_V = length(V_Temp);$
 - // Find the Score cut-off S, corresponding to the given P-value cut-off epsilon. $S = min \{Score_P (Score, L_U, L_V) \leq epsilon\};$
 - // Main Part
 - Construct a set CurrentSim of all local similarities within
 - // U_Temp and V_Temp, having P-value less than a cut-off epsilon
- 4 CurrentSim = SetLocalSim(b1, e1, b2, e2, epsilon);
- 5. IF (CurrentSim is NOT empty) // the similarities do exist
- 6. THEN // Extract the S-restricted backbone chain // CurrentBackboneChain for the set CurrentSim and // the P-value cut-off epsilon 7. CurrentBackboneChain= Chain R(CurrentSim, epsilon, S); 8. include CurrentBackboneChain into Backbone Chain: 9. Construct the series of boxes within the CurrentBox, which are separated with the local similarities from the CurrentBackboneChain; 10. include the boxes into WorkBoxList; ELSE 11. Construct a set AllWeakSim of all local similarities ; 12. within U_Temp and V_Temp, having P-value less than a cut-off P_Weak, which is "weaker" (i.e. larger) than epsilon; 13. Create an optimal (i.e. having maximal total score) chain of local similarities from AllWeakSim; 14. IF the optimal chain is significant as a whole 15. THEN include the chain into the WeakChainSet; 16.
- END_IF 17.
- 18 END IF
- END_ALGORITHM

Fig. 4. Algorithm Fractal (a) and its function ProceedBox (b).

(ii) the list of non-intersecting boxes WorkBoxList, which consists of all boxes to be processed.

We start with empty BackboneChain and with Work-BoxList, containing only the box corresponding to the whole initial sequences. To process the current box we first create the corresponding set of similarities CurrentLocSim (line 4, Figure 4b) and then extract the S-restricted backbone chain CurrentBackboneChain from the set (line 7). The procedure Chain_R (line 7) is described below. CurrentBackboneChain is not empty



Fig. 5. (a) A local similarity between pufferfish and human sequences found by OWEN \sim 2400 nucleotides upstream (in puffferfish sequence) of region E6 (Bagheri-Fam *et al.*, 2001). (b) A local similarity between chicken and human sequences that includes the start of KIAA1386 transcript.

because the set CurrentLocSim is not empty. Then we include similarities from the CurrentBackboneChain into the BackboneChain (step 8) and add the boxes corresponding to the intervals between the elements of the CurrentBackboneChain to the WorkBoxList (lines 9 and 10). If CurrentBackboneChain is empty (there are no ε -reliable similarities within the current box), a global alignment for the box (lines 12–17) may be of interest.

The number of boxes to be processed is no more than 2T + 1, where T is the number of similarities in the final backbone chain. Therefore, ProceedBox is called (line 8, Figure 4a) no more than 2T + 1 times, and the run-time of all lines in Figure 4a, except the line 8, is proportional to *T*.

To estimate the run-time of ProceedBox, consider the size M of the set CurrentSim of ε -reliable similarities within the current box. We cannot give a non-trivial (lower than proportional to the area of the box) general upper bound for M. However, in real situations M is small and depends mostly on ε (and not on the size of the box). To make this statement rigorous, one has to refine the definition of $P(S, L_1, L_2)$ and the probability model (including the hypothesis on the relations between the compared genomes). This is beyond the scope of the paper, and only an informal argument is presented here.

M can be represented as $M = M_b + M_r$ where M_b is a number of 'evolutionarily true' similarities in CurrentSim, and M_r is the number of random ε -reliable similarities. As long as ε is small, M_r is low, and M_b , since orthologous similarities are collinear, cannot be very high and declines with ε . Thus, the value of M and, therefore, the run-time of ProceedBox is a function $c(\varepsilon)$ and the total run-time of Fractal is $c(\varepsilon) \cdot T$.

Overview of algorithms Chain_Basic and Chain

Chain_Basic and Chain find the backbone set of similarities by processing similarities from R one by one in the order of their decreasing scores. For a current similarity *H* they answer two questions: (1) should *H* be added to the already built part $B = \{A_1, \ldots, A_s\}$ of the desired backbone chain? and (2) if yes, after which member of *B* should *H* be included?

Chain_Basic, applicable if similarities do not overlap, uses two global lists of similarities: (a) CurrentLocSim, which initially contains the provided set of similarities R; and (b) BackboneChain, which is initially empty, and at the end contains the desired backbone chain. To perform the search efficiently, we also support on BackboneChain the structure of 2–3-tree (Aho *et al.*, 1974).

When ε is small, overlaps of similarities should be rare. Still, they do occur. Algorithm Chain that finds the backbone chain when overlaps may be present is a straightforward generalization of Chain_Basic. Both algorithms can be seen at ftp://ftp.ncbi.nih.gov/pub/ kondrashov/owen/extra.

EXAMPLES

Let us see how the proposed hierarchical approach aligns sequences that are at different evolutionary distances from each other. Complete descriptions of the aligned sequences, alignments produced by OWEN, and alignments produced by PipMaker web server (Schwartz *et al.*, 2000; http://bio.cse.psu.edu/pipmaker) can be seen at ftp://ftp.ncbi.nih.gov/pub/kondrashov/owen/extra.

First, we aligned a region of pufferfish *Takifugu rubripes* genome (AF329945) that contains SOX9 locus to the orthologous segment of human genome. Comparison of these sequences performed previously using PipMaker (Bagheri-Fam *et al.*, 2001) revealed 5 conserved regions upstream of SOX9, and 3 conserved regions downstream of SOX9. OWEN detected all these regions, as well as > 20 local similarities outside them. Some extra similarities revealed by OWEN may be interesting (Figure 5a).

Second, we aligned a region of chicken *Gallus gallus* genome (AC094011) that contains loci AKAP450 (3'-part), CYP51, KRIT1, and KIAA1386 (5'-part) to its human ortholog. The backbone chain constructed by OWEN consists of 303 similarities. The chain of local similarities produced by PipMaker server (high sensitivity option) included less than 200 of similarities found by OWEN (including all exons) and very few extra similarities. Some of similarities revealed only by OWEN are biologically important (Figure 5b).

Finally, we aligned several orthologous regions of murine and human genomes. In this case, chains of local similarities found by PipMaker and OWEN are usually very close to each other (data not reported). This is not surprising, since these genomes are rather similar (Jareborg *et al.*, 1999).

DISCUSSION

We proposed a hierarchical, greedy approach to constructing chains of local similarities that describe overall correspondence between long, orthologous regions of moderately similar genomes. This approach is simple, efficient, and makes sense biologically.

Conceptually, resolving each essential pairwise conflict in favor of the better similarity is the simplest option. In contrast, the rationale behind the only reasonable alternative, seeking the optimal as a whole chain of similarities (Zhang *et al.*, 1994; Schwartz *et al.*, 2000), is obscure. Also, determining which chain is optimal requires assigning more or less arbitrary penalties for gaps between similarities.

Our algorithm Fractal is very efficient, due to two reasons. First, the run-time of creating the backbone chain for a set of N similarities is determined by the run-time of sorting it by scores. This can be done rapidly, in time $\sim N \cdot \log(N)$ or, under some natural conditions on the range of the scores (Aho *et al.*, 1974), even in time $\sim N \cdot \log \log(K)$ (where K is the highest score), by using priority queues (Johnson, 1982), stratified trees (van Emde Boas, 1977), or bounded ordered dictionaries (Melhorn and Nahler, 1990).

To find the optimal chain one has to use dynamic programming. Run-time of currently the most effective sparse dynamic programming (Eppstein *et al.*, 1992) depends on the data structure used to store the candidate points and can be $\sim N \cdot \log(N)$ (Chao *et al.*, 1995) or even $\sim N \cdot \log\log(L)$, where L is the length of the shorter sequence (Eppstein *et al.*, 1992). However, the multiplicative constant for sorting is smaller than for dynamic programming, since only one tree, instead of two is used and there is no need for extra operations (such as processing of intersections of boundaries between the candidates zones). In practice, both the backbone chain and the optimal chain can be found, from a provided set of similarities, very rapidly. OWEN (Ogurtsov *et al.*, 2002)

supports both these options.

Second, and more importantly, there is no need to construct all similarities when conflicts are resolved individually. Indeed, if we compare two sequences of length 10^7 (typical length of fragments of collinearity preserved between human and mouse genomes), finding all similarities requires a prohibitively high run-time \sim 10¹⁴ with a high constant. However, strong similarities can be found rapidly, as long as we assume that they contain even relatively short runs of matches. Thus, we can start from using 'core-based' (BLAST-like, Altschul et al., 1997) methods of finding local similarities, and perform exhaustive searches for weak similarities only within rectangles defined by strong similarities within the original $10^7 \times 10^7$ dot-matrix. This speeds up comparison of long sequences enormously. In contrast, if the optimal chain is sought, the whole dot-matrix must be scanned for even the weakest similarities that can potentially be included into this chain.

Biologically, it makes sense to keep a stronger similarity regardless of its conflicts with any number of weaker similarities since a stronger similarity is likely to reflect orthology (Figure 2). Of course, the backbone chain and the optimal chain may coincide, in particular, if similar sequences are compared.

In addition to relying exclusively on P-values, pairwise resolution of conflicts can also, as an option, be done manually. This makes it possible for an operator to use some hard-to-formalize clues for deciding which similarity to erase (and, perhaps, to store as a 'footnote' to the backbone chain, Ogurtsov *et al.*, 2002. As long as the decisions by the operator are transitive (i.e. it never happens that conflict between A_1 and A_2 is resolved in favor of A_1 , conflict between A_2 and A_3 in favor of A_2 , and conflict between A_1 and A_3 in favor of A_3), human interventions does not lead to any modification of our algorithms. Such intervention, which are hardly possible if an optimal chain is sought, may be very useful in practical work.

ACKNOWLEDGEMENTS

The authors thank four anonymous reviewers for many useful comments. Participation of M.A.R. in this and the accompanying paper was supported by INTAS grant 99-01476 by RFFI grant 00-04-48246 and by Netherland Organization for Scientific Research.

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